

# 1 **A hedonic approach to value *Pinus radiata* log traits for** 2 **appearance-grade lumber production**

## 3 4 **Abstract**

5 This study used a hedonic approach to estimate the economic value of radiata pine log attributes  
6 (small-end diameter, form and internode length) for appearance grade lumber, including Moulding  
7 & Better, Shop and Industrial Finger Joint. Models were also built at the tree level to investigate the  
8 effect of selection as conducted by breeders. A Chilean sawing study provided information on wood  
9 traits and log out-turn for 156 logs divided into three classes: pruned butt log, second log and third  
10 log. The conversion return of logs, instead of log prices, was used as the measure of log economic  
11 value. The economic values of log small-end diameter were 0.33, 0.19 and 0.10 US \$/mm for the  
12 first, second and third log respectively. Concerning form, those values were 2.6, 1.4 and 0.63 US \$  
13 for a marginal improvement of this characteristic. The value of mean internode length was 0.19 US  
14 \$/cm for second unpruned logs. Values for other internode length indices are also presented in this  
15 paper. Branch variables were not statistically significant in explaining the log recovery value.  
16 Finally, log recovery value was found to be elastic to the changes in small-end diameter and form,  
17 but inelastic to changes in the mean internode length.

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19 Key words: wood attributes; hedonic values; *Pinus radiata*; appearance lumber; breeding objectives.

## 20 **Introduction**

21 Log attributes, including volume and form, have a large influence on the yield and quality of  
22 lumber. Most attributes can be identified and measured, but their economic values are not well  
23 understood, nor are they frequently reported. For example, advances in the assessment of wood  
24 stiffness and resin defects of appearance products have contributed to improved log segregation  
25 practices (Lasserre et al. 2005; Lindström et al. 2002; McConchie and Cown 2008; Ridoutt et al.  
26 1999; Walker and Nakada 1999). The economic value of wood characteristics has received less

27 study. However, knowing the value of wood traits is very important if growers are to improve the  
28 quality of the forest crop.

29 Economic values are particularly important to tree breeders, as they require this information  
30 to define breeding objectives and to build selection indices. Commonly, bioeconomic models have  
31 been used to obtain those values, modeling the effects of trait changes on the profitability of a  
32 production system (Apiolaza and Garrick 2001; Borralho et al. 1993; Ivković et al. 2006). Other  
33 approaches used to obtain economic values of traits have been linear programming (Ladd and  
34 Gibson 1978), efficiency measures on production systems (e.g., Lambert and Wilson 2003;  
35 Todoroki and Carson 2003) and hedonic models (e.g., Bloomberg 2001).

36 Hedonic values are defined as the implicit prices of traits and they are revealed by observed  
37 prices of differentiated products and the specific amounts of traits associated with them (Lancaster  
38 1966; Rosen 1974). In the case of agricultural commodities, hedonic models have been applied to  
39 determine the marginal value of quality traits (Angel et al. 1990; Bowman and Ethridge 1992;  
40 Carew 2000; Espinosa and Goodwin 1991; Ethridge 1982; Ladd and Martin 1976; Nerlove 1995;  
41 Parker and Zilberman 1993; Walburger 2002).

42 When developing breeding objectives for specific wood attributes, comparable approaches  
43 to hedonic models have been occasionally applied under the name ‘value regressions’. For instance,  
44 Ernst and Fahey (1986) stated that regressions of value on wood traits, coming from product  
45 recovery studies, would provide the way to estimate economic weights for tree breeders. Similar  
46 studies have been documented by Cotterill and Jackson (1985) and Aubry et al. (1998). Forest  
47 hedonic models have mostly been concerned with the impact of environmental amenities on land  
48 prices (Bastian et al. 2002; Munn and Palmquist 1997; Snyder et al. 2007) and also with factors that  
49 explain stumpage price (e.g., Puttock et al. 1990).

50 This paper presents an application of hedonic models to value log and tree wood attributes  
51 for appearance lumber of *Pinus radiata* D.Don in Chile. The log recovery value is used as response

52 variable instead of log prices. Finally, the sensitivity of the log value to wood attribute changes is  
53 analyzed using an elasticity approach.

## 54 **Materials and methods**

55 The data for this project came from a Chilean sawing study that included 156 radiata pine logs from  
56 three stands. At the time of sampling the stands were 19, 22 and 34 years old with Site Indices of  
57 31, 28 and 27 m, respectively. These radiata pine stands are representative of the site quality  
58 available for clear wood production. The stands were thinned and pruned to different stocking  
59 intensities, but all of them targeted a 5 m long pruned log. Trees used in the current study, were  
60 chosen considering representativeness in the diameter distribution as well as stem quality to  
61 generate sawlogs. The log sample contained a minimum small-end diameter of 20 cm and most  
62 trees contained three 5 m logs. Table 1 summarizes quality information at the log level.

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78 Table 1: Average value of log descriptors segregated by log class.

Variable	Pruned butt log	Second log	Third log
Number of logs	54	57	45
Log length (LL, cm)	505	505	410
Small-end diameter (SED, mm)	385.15	358.60	335.09
Log volume (VOL, m <sup>3</sup> )	0.73	0.55	0.43
Form (FORM)	0.73	0.79	0.79
Defect core diameter (DCD, mm)	240.69		
Pruned log index (PLI)	4.83		
Branch index (BI, mm)		44.95	50.46
Largest branch (LB, mm)		56.64	66.55
Base internode length (BIL, cm)		71.31	52.42
Mean internode length (MIL, cm)		71.44	58.12
Internode index base 80 cm (II <sub>80</sub> , %)		33.04	23.49
Internode index base 60 cm (II <sub>60</sub> , %)		46.77	32.16

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107 **Definition of tree and log variables**

108 Variable SED, presented in Table 1, is the small-end diameter of the log. FORM corresponds to the  
109 relationship  $Cvol/Lvol$ , where  $Cvol$  is the common volume ( $m^3$ ) equivalent to the maximum  
110 cylinder contained in the log, and  $Lvol$  is the under bark log volume. SED and FORM are related to  
111 the recovery of solid wood during log processing. Branch index (BI) is the mean diameter of the  
112 four largest branches of the log, one per quadrant (North, East, West and South). Largest Branch  
113 (LB) is the diameter of the largest branch of the log. Defect core diameter (DCD) corresponds to the  
114 diameter with defects after pruning. The prune log index (PLI) is an indicator that expresses the  
115 potential of a pruned log to produce long clear wood pieces, such as Moulding & Better (Park  
116 1989). PLI is estimated by the following relationship:

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$$PLI = (D1.3 - DCD)^{0.5} * (D1.3/DCD) * FORM^{1.6} \quad (1)$$

118 where D1.3 is the diameter at 1.3 m of log. Usually, the DCD is known after processing the log;  
119 nevertheless, it can be previously estimated using PLI, or by statistical models that consider  
120 variables related to the silvicultural regime of the stand (Knowles et al. 1987).

121 Internode length is an important characteristic in determining the out-turn of Shop and Finger  
122 Joint grades. The mean internode length (MIL) is the sum of length (m) of internodes in branched  
123 section of the log divided by the number of internode lengths in branched section of the log (Watt et  
124 al. 2000). Internode index ( $II_b$ ) is the sum of internode lengths greater than a given base (b) divided  
125 by the log length. This study considered bases of 60 and 80 cm. Further details relating to the above  
126 traits are described in the literature by Park (1989), Grace and Carson (1993), Carson and Inglis  
127 (1988) and Jayawickrama et al. (1997). The base internode length (BIL) corresponds to the  
128 minimum internode length that is contained in 50 percent of the log length. Meneses and Guzman  
129 (2003) developed this index for unpruned logs based on the Internode index ( $II_b$ ). Thus, BIL  
130 represents that minimum internode length (b) that generates an  $II_b$  equal to 0.5.

131  $II_b$ , MIL and BIL give complementary information about internode length. MIL describes the  
132 average internode length of a log, tree or stand while  $II_b$  provides an indication of variability but it is  
133 usually estimated for specific internode lengths, which limits the possibilities of processing to a

134 limited set of products. BIL is more flexible and is associated to the length of clear pieces that could  
135 be obtained from the logs, which is useful for matching stands of varying internode length to  
136 product requirements (Meneses and Guzmán 2003).

137 All the variables included in this study were expected to have an effect on the log value  
138 recovery.

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160 Table 2: Descriptive statistics of lumber volume (m<sup>3</sup>) by product.

	Moulding & Better (m <sup>3</sup> )	3 <sup>rd</sup> Clr (m <sup>3</sup> )	Shop 1 (m <sup>3</sup> )	Shop 2 (m <sup>3</sup> )	Shop 3 (m <sup>3</sup> )	Finger Joint Blocks (m <sup>3</sup> )	Finger Out 161 (m <sup>3</sup> )
<b>Pruned butt log</b>							
Average	0.179	0.002	0.036	0.045	0.070	0.020	0.022
Maximum	0.613	0.052	0.135	0.191	0.167	0.111	0.063
Minimum	0.000	0.000	0.000	0.000	0.000	0.000	0.000
Standard deviation	0.147	0.009	0.041	0.046	0.038	0.029	0.024
<b>Second log</b>							
Average	0.027	0.005	0.035	0.083	0.103	0.016	0.030
Maximum	0.371	0.091	0.233	0.388	0.296	0.142	0.095
Minimum	0.000	0.000	0.000	0.000	0.000	0.000	0.000
Standard deviation	0.069	0.018	0.058	0.089	0.056	0.028	0.282
<b>Third log</b>							
Average	0.001	0.001	0.014	0.137	0.086	0.032	0.026
Maximum	0.025	0.037	0.221	0.413	0.267	0.123	0.065
Minimum	0.000	0.000	0.000	0.000	0.000	0.000	0.000
Standard deviation	0.005	0.006	0.043	0.110	0.059	0.033	0.020
<b>Tree</b>							
Average	0.239	0.010	0.096	0.208	0.244	0.068	0.075
Maximum	1.009	0.091	0.442	0.632	0.507	0.178	0.203
Minimum	0.028	0.000	0.000	0.000	0.000	0.000	0.000
Standard deviation	0.242	0.026	0.114	0.193	0.099	0.056	0.057

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190 **Sawmill product evaluation**

191 Once the standing trees and logs were assessed in the field, the logs were processed at the mill. The  
192 aim of processing was to maximize the recovery of lumber in the Moulding & Better grades from  
193 the pruned logs and Shop grades from unpruned logs, as described by the Western Wood Products  
194 Association for the USA market (WWPA 1995). An additional low quality product called Finger  
195 Out was generated by the sawing study and included in the analysis. Lumber grade recovery for  
196 each log type is shown in Table 2.

197 **Model components**

198 Hedonic models (HM) disaggregate the price of a product into the value of its component traits to  
199 obtain the contributory value of each attribute (Rosen, 1974).

200 Logs are required by processors because they contain wood traits to produce specific  
201 lumber. In keeping with HM theory, the log is a differentiated product with attributes can be  
202 identified and measured and, therefore monetarized.

203 We assume competitive markets, and the models developed by Ladd and Martin (1976) and  
204 Espinosa and Goodwin (1991) are used as a theoretical framework. We also consider a single  
205 product firm where specific log attributes, such as small-end diameter, form and internode length,  
206 are arguments in the appearance-grade lumber production function  $G(t)$ .

207 If the log processor is assumed to maximize profit subject to the production function  $G(t)$ ,  
208 the first order conditions of the profit maximization generate Equation (2) which represents a  
209 hedonic price function. Lumber production is a function of the log trait use, which is a function of  
210 the log use; thus, the differentiation of a compound function (function that operates on another  
211 function, often represented as nested functions e.g.  $f(g(x))$ ) is used to derive Equation (2).

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$$p_z = p * \sum_{i=1}^n \frac{\partial G}{\partial t_i} * \frac{\partial t_i}{\partial z} \quad (2)$$

213 where  $p_z$  is the price paid for the input (log) and  $p$  is the price received for the product (appearance-  
214 grade lumber). Variable  $z$  corresponds to the quantity of the input log used in the production of

215 lumber,  $t_i$  is the amount of trait  $i$  provided by one unit of input  $z$ ,  $\frac{\partial t_i}{\partial z}$  is the marginal yield of trait  $t_i$   
 216 in the production of lumber from input  $z$ , and  $p * \frac{\partial G}{\partial t_i}$  is the value of the marginal product of trait  $t_i$ ,  
 217 which represents the marginal implicit price (hedonic price) paid for the trait  $t_i$  because of its  
 218 contribution to lumber production. Thus, Equation 2 states that the price paid for the input log is  
 219 equal to the sum of the hedonic prices of the log traits multiplied by the marginal yield of those  
 220 traits.

221 Equation 2 may be simplified with the assumption that the marginal product of the trait  $t_i$   
 222 and  $\frac{\partial t_i}{\partial z} = T_i$  are constant. This simplification implies that each additional unit of input  $z$  contributes  
 223 the same amount of the  $t$ -th trait to the function  $G(t)$ , and the marginal hedonic value of trait  $t$  is  
 224 constant (Espinosa and Goodwin 1991; Ladd and Martin 1976). Thus, Equation (2) can be written  
 225 as the following single linear hedonic price function:

$$226 \quad p_z = \sum_{i=1}^n \beta_{t_i} * T_i \quad (3)$$

227 Equation (3) is showing that every extra unit of input  $z$  contributes the same quantity of the  $t$ -th  
 228 trait to the production function  $G(t)$ , and that the hedonic price of the log attributes are constant.  
 229 These assumptions have been consistent with many natural commodity traits (Ladd and Martin  
 230 1976). Nevertheless, this study is open to estimate nonlinear functional forms according to the  
 231 model specification tests.

232 Linking log prices with their attributes by regressions allows obtaining the parameters of  
 233 Equation (2), which is the foundation of hedonic models.

234 If attributes are not reflected in prices, but they are observable, measurable and directly  
 235 related to the quality and value of final products, an alternative approach of value could be used in  
 236 order to estimate the parameters of Equation (2). For example, log internode length is a trait  
 237 intimately related to quality and prices of Shop products. Thus, longer internodes generate longer

238 Shop pieces with higher prices. However, the log market does not explicitly value this  
239 characteristic in unpruned log prices.

240 This study proposes the use of a log recovery value called *conversion return* (CR), which  
241 represents the theoretical maximum willingness to pay for logs in US \$/m<sup>3</sup> delivered to the sawmill  
242 (Davis et al. 2004). The suitability of product recovery studies to value wood traits for breeding  
243 purposes has been reported by other studies (e.g., Aubry et al. 1998; Ernst and Fahey 1986). This  
244 indicator corresponds to the residual value of the log after processing, and it is estimated as follows:

$$245 \quad CR = \sum_{i=1}^N p_i * L_i - PC \quad (4)$$

246 where  $p_i$  is the price of lumber type  $i$ ,  $L_i$  is the volume of lumber type  $i$  contained in one cubic  
247 meter of logs, and  $PC$  is the processing cost of one cubic meter of logs. Prices of lumber  
248 corresponding to the “Industrials, Specialties, and other items” section in the Random Lengths  
249 Report (Random Lengths 2008), were directly provided by Random Lengths publications. These  
250 corresponded to the monthly prices series 1995-2008, which were expressed in 2008 using the USA  
251 CPI (base 1982-1984:100). The average values of these series were used to estimate the CR. Table  
252 3 presents prices and shipping costs of products, as well as log processing costs (Jean P. Lasserre,  
253 pers. comm., Forestal Mininco-Chile, March 20, 2008).

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264 Table 3: Prices and shipping costs for products and processing costs for logs.

Moulding & Better [US\$/m <sup>3</sup> ]	3 <sup>rd</sup> Clr [US \$/m <sup>3</sup> ]	Shop 1 [US \$/m <sup>3</sup> ]	Shop 2 [US \$/m <sup>3</sup> ]	Shop 3 [US \$/m <sup>3</sup> ]	Finger Joint Bloks [US \$/m <sup>3</sup> ]	Finger Out [US \$/m <sup>3</sup> ]	Shipping cost [US \$/m <sup>3</sup> ]	Log processing cost [US \$/m <sup>3</sup> ]
584	394	373	328	266	367	257	60	70

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288 Explanatory variables were measured and estimated from logs and trees. The information at  
289 the log level includes SED, FORM, internode indices (MIL, BIL, II<sub>60</sub>, II<sub>80</sub>) and branch measures.  
290 However, our hypothesis was that branches would have only a minor influence on the quality and  
291 value of appearance products, because the knots are removed as part of the production process – i.e.  
292 a remanufacturing plant will use chop saws to remove all knots. Thus the size of knots has a much  
293 lower effect than the distribution of knots, which is considered by the internode index. In fact, the  
294 requirements for radiata pine appearance lumber relate only to the length of the clear piece  
295 (Kretschmann and Hernandez 2006). If there were specific stiffness or strength requirements, the  
296 situation would be different because in that case knots derived of branches would cause downgrade  
297 in lumber, as it happens with structural lumber (Chauhan 2006).

298 At the tree level, the explanatory variables were diameter at breast height (DBH) and  
299 internode length indices. Tree form, BI and products volume per tree were obtained by aggregating  
300 the logs for each tree, which meant rebuilding forty trees.

301 The suitability of a linear functional form for the hedonic models was assessed by the Box-  
302 Cox transformation (1964). The objective of this transformation is to identify an appropriate  
303 exponent lambda ( $\lambda$ ) to obtain the best transformation to achieve data normality. The Box-Cox  
304 transformation takes the following form:

$$305 \quad y(\lambda) = \begin{cases} \frac{y^\lambda - 1}{\lambda}, & \text{if } \lambda \neq 0; \\ \log y, & \text{if } \lambda = 0. \end{cases} \quad (5)$$

306 The resulting functional form will depend on the value of  $\lambda$ . For instance, if  $\lambda$  is equal to one  
307 the transformation is linear.

308 The hedonic model approach allows estimation of elasticities to assess the sensitivity of log  
309 value to changes in wood attributes. The changes in log value and attributes were expressed as  
310 percentages of the average log value and average trait. The elasticity of log value ( $\epsilon$ ) is the change  
311 in CR divided by the change in the attribute, multiplied by the level of the attribute divided by the

312 level of CR. In this way, the elasticity depends on the attributes levels considered in its estimation.  
313 Elasticity of log value ( $\epsilon$ ) is estimated as follows:

$$314 \quad \epsilon_i = \frac{\partial CR}{\partial t_i} * \frac{t_i}{CR} \quad (6)$$

315 where  $t_i$  is a trait in the hedonic model and  $CR$  is the conversion return of the log. If this elasticity  
316 is lower than one (inelastic), there will be a less than proportionate change in relative log value for  
317 any change in the wood trait. The opposite is true if the elasticity is greater than one (elastic), when  
318 the proportionate change in relative log value is greater than the change in the trait. Thus, it is  
319 desirable that the log attributes that contribute to log value, such as SED, FORM and internode  
320 length, have elasticities values greater than one.

## 321 **Results and discussion**

322 Hedonic models were fit at the log level and tree level, considering attributes of form, diameter,  
323 internode length and branches, as well as of silviculture. The hedonic value of a given attribute was  
324 calculated as the partial derivative of CR on that attribute. Models presented at the tree level aim to  
325 understand the effect of improving wood quality as done by tree breeders in the development of  
326 breeding objectives. Furthermore, there is rarely an opportunity in radiata pine to process 14 m of  
327 tree for the same end-product. This information could help to assess the effect of improvement at  
328 the tree-level on profitability at the log-level.

### 329 **Log level models**

330 The conversion return averaged 114, 66 and 54 US \$/m<sup>3</sup> for first, second and third logs  
331 respectively. Log recovery values were consistent with the amount of highest priced lumber that  
332 they generated. Thus, the butt log presented the highest value due to its high volume of Moulding &  
333 Better products. However, higher differences in value between butt log and second log have been  
334 reported (e.g., Beauregard et al. 2002). The smaller difference obtained in this study was due to  
335 small piece size, large defect core size, and the associated low PLI (4.8). BI for the second log was  
336 45 mm, lower than for the third log (50 mm). However, the largest branch was found in the second

337 log (158 mm). Similar results were obtained by Woollons et al. (2002) in a study for developing a  
338 branch model for New Zealand radiata pine. In addition, the author highlights the variability of  
339 branch size observed for this species. The high variability of radiata pine branching traits, within  
340 trees and among trees, was also reported by Bannister (1962).

341 Branch size depends on initial spacing and site index (Tombleson et al. 1990). In addition,  
342 the combined effects of thinning and pruning, could increase branch sizes above the last pruned  
343 section (Jacobs 1938 cited by Shirley 1974). This situation could occur when wider spacing is left  
344 after thinning, especially in direct sawlog regimes (Chauhan 2006).

345 Branch data for second and third logs showed a weak (not significant) correlation between BI  
346 and MIL, of 0.02 and 0.16 for the second and third log respectively. Considering LB these  
347 correlations increased slightly. Our data set does not support the positive relationship between  
348 internode length and branch size reported by other studies (e.g., Burdon et al. 1992; Watt et al.  
349 2000). In contrast, Woollons et al. (2002) obtained a low correlation (around 0.1) between the size  
350 of the maximum branch and internode length. Nevertheless, our data showed a positive correlation  
351 between BI and SED, 0.53 and 0.47 for second and third log respectively.

352 Longer internodes were observed in the second log, a result that agrees with the trend  
353 depicted by the model of Grace and Carson (1993) and with the results obtained by Tombleson et  
354 al. (1990).

355 There were six hedonic models fitted at the log level: one for the first pruned log, four for the  
356 second unpruned log and one for the third unpruned log. The explanatory variables for the first log  
357 were FORM, SED and DCD. For the second log the variables were SED, FORM, BI and one  
358 internode measure at the time: MIL, BIL,  $II_{80}$  and  $II_{60}$ . Finally, the third log model considered SED,  
359 FORM and BIL as independent variables.

360 The functional form of the hedonic models was assessed by the Box-Cox transformation,  
361 obtaining  $\lambda=1$  for all models and making a linear functional form suitable.

362 Models were not found to be heteroskedastic using the White Test, at a significance level of  
363 0.01. The normality of the data was also tested using the Shapiro-Wilk test. Results indicated that  
364 there was no evidence to reject the null hypothesis of normally distributed data. Collinearity  
365 between explanatory variables was tested by the condition index (CI). This index is a measure of  
366 the relative amount of variance associated with an eigenvalue; consequently, a big CI indicates a  
367 high level of collinearity (Quinn and Keough 2002; Rawlings et al. 1998). Table 4 indicates the  
368 presence of collinearity, especially with variables related to branches and internode length.

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388 Table 4. Condition index (CI) to test collinearity in models at the log level.

Variables	Model Log 1	Model 1 Log 2	Model 2 Log 2	Model 3 Log 2	Model 4 Log 2	Model Log 3
	CI	CI	CI	CI	CI	CI
INTERCEPT	1.000	1.000	1.000	1.000	1.000	1.000
SED	9.624	5.195	4.040	4.424	4.519	4.156
F	19.713	7.541	7.320	7.968	7.021	9.742
DCD	34.347					
BI		30.329	29.898	30.245	29.733	
MIL		12.400				
BIL			12.2881			35.524
$\Pi_{60}$				12.338		
$\Pi_{80}$					12.154	

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410           The first approach to reduce collinearity was to eliminate those variables with highest values  
411 of CI. However, collinearity persisted with the internode length variables, which presented a CI  
412 close to 27 in the unpruned log models. Instead, models were fitted centering the explanatory  
413 variables, expressing them as deviations from their mean values. Using this approach, the CI for  
414 explanatory variables was reduced to less than three, which would suggest no collinearity problems.  
415 This centering process does not affect residual standard deviations, goodness of fit, coefficient  
416 values or standard error of the interactions, but its main effect is that the coefficients are now  
417 interpretable based on a comparison to the mean of the data (Gelman and Hill 2007).

418           Models were also tested with the Durbin-Watson statistic ( $d$ ) to detect autocorrelation in the  
419 residuals. The statistic  $d$  was greater than 2 for all log models suggesting that there are no  
420 autocorrelation problems.

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436 Table 5. Hedonic model results, first, second and third log.

Models	Parameter Estimate	Standard Error	R <sup>2</sup> -adj
<b>Pruned butt log</b>			
$CR = \beta_0 + \beta_1 * SED + \beta_2 * FORM + \beta_3 * DCD$			0.65
Intercept	113.656***	2.103	
SED	0.339***	0.059	
FORM	257.900***	55.602	
DCD	-0.267***	0.090	
<b>Second log, model 1</b>			
$CR = \beta_0 + \beta_1 * SED + \beta_2 * FORM + \beta_3 * MIL + \beta_4 * BI$			0.66
Intercept	66.331***	2.690	
SED	0.189***	0.033	
FORM	145.515***	36.191	
MIL	0.187**	0.080	
BI	-0.043	0.172	
<b>Second log, model 2</b>			
$CR = \beta_0 + \beta_1 * SED + \beta_2 * FORM + \beta_3 * BIL + \beta_4 * BI$			0.68
Intercept	66.336***	2.628	
SED	0.191***	0.033	
FORM	142.491***	35.376	
BIL	0.159***	0.056	
BI	0.003	0.169	
<b>Second log, model 3</b>			
$CR = \beta_0 + \beta_1 * SED + \beta_2 * FORM + \beta_3 * \Pi_{60} + \beta_4 * BI$			0.65
Intercept	66.299***	2.716	
SED	0.200***	0.034	
FORM	147.076***	36.544	
$\Pi_{60}$	22.572**	10.833	
BI	-0.003	0.176	
<b>Second log, model 4</b>			
$CR = \beta_0 + \beta_1 * SED + \beta_2 * FORM + \beta_3 * \Pi_{80} + \beta_4 * BI$			0.67
Intercept	66.271***	2.636	
SED	0.191***	0.033	
FORM	149.179***	35.486	
$\Pi_{80}$	27.518***	9.887	
BI	-0.033	0.168	
<b>Third log</b>			
$CR = \beta_0 + \beta_1 * SED + \beta_2 * FORM + \beta_3 * BIL$			0.38
Intercept	54.159***	2.109	
SED	0.099***	0.025	
FORM	62.880*	32.166	
BIL	0.025	0.065	

\* Significant at 0.1 level; \*\* significant at 0.05 level; \*\*\* significant at 0.01 level.

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444 Table 5 presents the results of the final models. Given the linear functional form of the  
445 models, parameters correspond to the trait hedonic values.

446 The model for the pruned butt log presented an  $R^2$ -adj of 0.65 and all coefficients were  
447 significantly different from zero ( $p < 0.01$ ). As expected, FORM and SED had a positive contribution  
448 to log value, while DCD had a negative role. For this log, 50 percent of the CR variation was  
449 explained by SED ( $p < 0.0001$ ), which supports the economic importance of log size. FORM and  
450 SED are inherent attributes of the logs, whereas DCD is a variable generated by silviculture.  
451 Despite this difference, DCD was considered in the model because it gives indirect information of  
452 the amount of knot-free wood, which is the objective product in the pruned log.

453 The hedonic values of SED and DCD were 0.33 and -0.27 US \$/mm respectively. These  
454 values would correspond to the marginal contribution to log recovery value for having an extra  
455 millimeter on SED and DCD, in which case they are expressed in US \$/m<sup>3</sup>. The variable FORM is  
456 an index that ranges between 0 and 1, thus improving this index by 1 percent would result in an  
457 increment of 2.58 US \$/m<sup>3</sup> in the log conversion return.

458 The models for second logs presented high values for  $R^2$ -adj. (see Table 5). All parameters  
459 were statistically significant ( $p < 0.05$ ) and their signs were consistent across models. Additionally,  
460 the magnitude of the coefficients for internode indices followed the expected trend; the highest  
461 value is associated with  $II_{80}$  followed by  $II_{60}$ . Similar results were obtained by Beauregard et al.  
462 (2002) but their model considers DBH, BI and  $II_{60}$  as explanatory variables and the resulting  
463 goodness of fit was 0.9. The authors did not report the regression coefficients; nevertheless, they  
464 pointed out that trees with small branches presented better grade recovery than trees with big  
465 branches.

466 In the second logs the hedonic values for FORM were consistent across models with values  
467 between 1.46 and 1.49 US \$/m<sup>3</sup>. These values were lower than those observed in the first log. This  
468 result was expected, due to the higher economic value of the butt log. In fact, 65 percent of the tree  
469 value was contained in the first log.

470 SED presented a consistent hedonic value around 0.19 US \$/m<sup>3</sup> across models, explaining 65  
471 percent of variation of the CR (p<0.0001).

472 Regarding the economic value of internodes, the first model fitted MIL with a hedonic value  
473 of 0.19 US \$/cm. The hedonic value for BIL was 0.16 US \$/cm. Internode indices II<sub>60</sub> and II<sub>80</sub>  
474 presented values corresponding to marginal contributions of 0.23 and 0.28 US \$/m<sup>3</sup> to the CR,  
475 respectively.

476 Branch variables did not provide a significant (p<0.1) explanation of recovery value for  
477 second logs for appearance lumber. Table 5 shows the information corresponding to BI; models  
478 were also tried with LB, which was not significant (p<0.1).

479 Concerning the third log, 32 percent of CR variation was explained by SED which supports  
480 the significant economic weight of this trait (p<0.0001). Although, the goodness of fit was poor  
481 (R<sup>2</sup>-adj 0.38) the intercept and parameters associated with SED and FORM were significant (p<0.1)  
482 and the corresponding hedonic values were lower than those obtained for the second log. The  
483 parameter associated to BIL was not significant; however, its sign was consistent with expectations.  
484 Additionally, this log presented the highest variability of quality and value amongst logs, which  
485 could be influencing fit.

#### 486 ***Tree level models***

487 Two models are presented in order to explain tree value in terms of wood attributes. The  
488 functional form of these models was also linear, with  $\lambda=1$  for the Box-Cox transformation. These  
489 models did not present heteroskedasticity problems; nevertheless, there was collinearity between  
490 explanatory variables, which was avoided by centering the variables. Concerning autocorrelation,  
491 the Durbin-Watson statistic (*d*) was close to 1.9 for both tree models; which would indicate a mild  
492 presence of autocorrelated residuals.

493 The average conversion return was 175 US \$/tree. Models that explained CR at the tree level  
494 resulted in an improved fit compared to the models at the log level, with an R<sup>2</sup>-adj. of 0.92 for both  
495 models, respectively. Table 6 presents the results of the hedonic models at the tree level.

496 Table 6. Hedonic models at the tree level

Models	Parameter Estimate	Standard Error	R <sup>2</sup> -adj
Tree, model 1			
CR = $\beta_0 + \beta_1 * DBH + \beta_2 * FORM + \beta_3 * MIL_{511}$			0.92
Intercept	175.445***	5.786	
DBH	1.091***	0.092	
FORM	381.197**	144.251	
MIL <sub>511</sub>	0.115	0.174	
DCD	-0.011	0.159	
BI	-0.115	0.366	
Tree, model 2			
CR = $\beta_0 + \beta_1 * DBH + \beta_2 * FORM + \beta_3 * BIL_2$			0.92
Intercept	175.44***	5.556	
DBH	1.049***	0.092	
FORM	374.453**	138.323	
BIL <sub>2</sub>	0.213*	0.116	
DCD	0.054	0.158	
BI	-0.078	0.350	

\* Significant at 0.1 level; \*\* significant at 0.05 level; \*\*\* significant at 0.01 level.

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514 The explanatory variables considered in these models were DBH, FORM, internode  
515 measures, DCD and BI. The pertinence of DBH and internode length for predicting appearance  
516 lumber quality from trees has been also reported by Gazo et al. (2000).

517 Concerning internode measures, model 1 considered the mean internode length between 5  
518 and 11 m (MIL<sub>511</sub>). The second model included the base internode length of the second log as  
519 explanatory variable (BIL<sub>2</sub>).

520 The economic values of attributes derived from model 1 were 1.09 US \$/cm for DBH and  
521 3.81 US \$ for FORM (the highest value for this variable). The value of MIL<sub>511</sub> was not significant,  
522 although its magnitude and sign were as expected. In the same way, DCD and BI were not  
523 significant to explain tree recovery value. In model 2, variables DBH and FORM had similar  
524 hedonic values to those generated by model 1. The parameter associated to BIL<sub>2</sub> was statistically  
525 significant ( $p < 0.1$ ) and higher than the corresponding value at the log level. This difference is due  
526 to the higher economic value of trees compared with the value of second logs. In contrast, DCD and  
527 BI were not significant and close to zero.

528 Although the value of trees could be debatable, they were estimated to show the joint value  
529 of the logs that potentially could be processed for appearance products. This information could be  
530 useful for breeders, particularly to assess single-purpose versus multi-purpose breeding programs.

### 531 ***Elasticity results***

532 The sensitiveness of CR to log attributes changes can be analyzed using elasticity. Despite of the  
533 similarity between the elasticity of CR and the attribute economic value, they are different concepts.  
534 The value of an attribute obtained by hedonic models corresponds to the marginal contribution of  
535 the trait to the CR and it is expressed in absolute values (US \$/m<sup>3</sup>). The elasticity of the CR with  
536 respect to one log trait is the percentage change in CR caused by a one percent change in the trait.  
537 The changes in CR and attributes are expressed as percentages of the average CR and average  
538 attribute. Elasticity is dimensionless and its interpretation depends on the resulting value being  
539 greater, equal or lower than one.

540 Table 7 presents the elasticities of the log recovery value estimated from two hedonic  
541 models. The first one corresponds to the model of the butt log, while the second one is model 1 for  
542 the second log (see Table 5). Elasticity of log recovery value was estimated for SED, FORM, DCD  
543 and MIL. The elasticity values for the pruned butt log indicate that the CR is SED and FORM  
544 elastic, but DCD inelastic. Thus, CR would increase by 1.2 percent if SED experiments a change of  
545 1 percent, while CR would increase by 1.7 percent for FORM. Concerning DCD, a change in this  
546 variable would cause a less than proportional change in CR. Given that this variable has a negative  
547 contribution to the log CR, having elasticity lower than one is advantageous.

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566 Table 7. Elasticities for log conversion return on attributes SED, FORM, DCD and MIL.

Models	Mean attributes values	Elasticity (%)
<u>Pruned butt log model</u>		
SED (mm)	385.148	1.149
FORM	0.730	1.656
DCD (mm)	240.685	-0.565
<u>Second log, model 1</u>		
SED (mm)	358.596	1.027
FORM	0.792	1.737
MIL (cm)	70.786	0.201

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587           Concerning the second log, the CR resulted to be SED and FORM elastic, with similar  
588 elasticity values to the butt log. On the other hand, CR resulted to be MIL inelastic. Thus, the CR  
589 would increase just by 0.2 percent if the mean internode length increased by 1 percent.

590           Elasticity values could be useful complementary information to implement wood attribute  
591 rankings in breeding programs. For instance, if a wood attribute has high economic value and its log  
592 value elasticity is higher than one, then this characteristic will reward breeding effort, as it happens  
593 with SED and FORM.

## 594 **Conclusions**

595           The objective of this study was to estimate the economic value of wood traits of radiata pine logs  
596 for producing appearance lumber (Moulding & Better, Shop and Industrial Finger Joint). We used  
597 hedonic models to ascertain the economic values of wood attributes on pruned butt logs, unpruned  
598 logs and trees. Finally, an elasticity analysis was used to understand the magnitude and the direction  
599 of the log recovery value response due to changes in wood attributes.

600           The use of conversion return as response variable made it possible to capture and value  
601 marginal changes in wood traits. Thus, despite of its theoretical nature, conversion return is a  
602 plausible economic measure to assess wood traits at the log and tree level. Using conversion return,  
603 processors incorporate information known that is part of their decision making process when buying  
604 logs.

605           SED and FORM were the characteristics with the highest economic value for the production  
606 of appearance lumber, as well as generating the highest log value elasticities. This result is  
607 consistent with the priorities observed in many breeding programs. The value of internode length  
608 indices highlighted their significant contribution to the value of logs destined to appearance lumber.

609           Branch variables did not contribute to explain the variation of CR for unpruned logs. These  
610 results supported the hypothesis asserted in this study. In this way, the wood quality of unpruned  
611 logs to produce appearance grades should be just focussed on SED, FORM and internode length

612 variables. In addition, appearance products have no requirements for stiffness and strength, a case in  
613 which knots generated by branches would negatively affect the log recovery value.

614 BIL showed a good performance at explaining log and tree recovery values. Thus, it would  
615 be advantageous to incorporate this alternative index to the information derived from radiata pine  
616 unpruned logs.

617 The elasticity analysis was useful to examine the responsiveness of log value to changes in  
618 wood characteristics. The elasticity of the conversion return, due to changes in log attributes could  
619 be complementary information for ranking trees in breeding programs.

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